

# Fractions and Decimals

## 2.1 INTRODUCTION

You have learnt fractions and decimals in earlier classes. The study of fractions included proper, improper and mixed fractions as well as their addition and subtraction. We also studied comparison of fractions, equivalent fractions, representation of fractions on the number line and ordering of fractions.

Our study of decimals included, their comparison, their representation on the number line and their addition and subtraction.

We shall now learn multiplication and division of fractions as well as of decimals.

## 2.2 HOW WELL HAVE YOU LEARNT ABOUT FRACTIONS?

A **proper fraction** is a fraction that represents a part of a whole. Is  $\frac{7}{4}$  a proper fraction?

Which is bigger, the numerator or the denominator?

An **improper fraction** is a combination of whole and a proper fraction. Is  $\frac{7}{4}$  an improper fraction? Which is bigger here, the numerator or the denominator?

The improper fraction  $\frac{7}{4}$  can be written as  $1\frac{3}{4}$ . This is a **mixed fraction**.

Can you write five examples each of proper, improper and mixed fractions?

**EXAMPLE 1** Write five equivalent fractions of  $\frac{3}{5}$ .

**SOLUTION** One of the equivalent fractions of  $\frac{3}{5}$  is

$$\frac{3}{5} = \frac{3 \times 2}{5 \times 2} = \frac{6}{10}. \text{ Find the other four.}$$

**EXAMPLE 2** Ramesh solved  $\frac{2}{7}$  part of an exercise while Seema solved  $\frac{4}{5}$  of it. Who solved lesser part?

**SOLUTION** In order to find who solved lesser part of the exercise, let us compare  $\frac{2}{7}$  and  $\frac{4}{5}$ .



Converting them to like fractions we have,  $\frac{2}{7} = \frac{10}{35}$ ,  $\frac{4}{5} = \frac{28}{35}$ .

Since  $10 < 28$ , so  $\frac{10}{35} < \frac{28}{35}$ .

Thus,  $\frac{2}{7} < \frac{4}{5}$ .

Ramesh solved lesser part than Seema.

**EXAMPLE 3** Sameera purchased  $3\frac{1}{2}$  kg apples and  $4\frac{3}{4}$  kg oranges. What is the total weight of fruits purchased by her?

**SOLUTION** The total weight of the fruits =  $\left(3\frac{1}{2} + 4\frac{3}{4}\right)$  kg

$$= \left(\frac{7}{2} + \frac{19}{4}\right) \text{ kg} = \left(\frac{14}{4} + \frac{19}{4}\right) \text{ kg}$$

$$= \frac{33}{4} \text{ kg} = 8\frac{1}{4} \text{ kg}$$



**EXAMPLE 4** Suman studies for  $5\frac{2}{3}$  hours daily. She devotes  $2\frac{4}{5}$  hours of her time for Science and Mathematics. How much time does she devote for other subjects?

**SOLUTION** Total time of Suman's study =  $5\frac{2}{3}$  h =  $\frac{17}{3}$  h

Time devoted by her for Science and Mathematics =  $2\frac{4}{5} = \frac{14}{5}$  h

$$\begin{aligned} \text{Thus, time devoted by her for other subjects} &= \left(\frac{17}{3} - \frac{14}{5}\right) \text{ h} \\ &= \left(\frac{17 \times 5}{15} - \frac{14 \times 3}{15}\right) \text{ h} = \left(\frac{85 - 42}{15}\right) \text{ h} \\ &= \frac{43}{15} \text{ h} = 2\frac{13}{15} \text{ h} \end{aligned}$$



**EXERCISE 2.1**

1. Solve:

- (i)  $2 - \frac{3}{5}$       (ii)  $4 + \frac{7}{8}$       (iii)  $\frac{3}{5} + \frac{2}{7}$       (iv)  $\frac{9}{11} - \frac{4}{15}$
- (v)  $\frac{7}{10} + \frac{2}{5} + \frac{3}{2}$       (vi)  $2\frac{2}{3} + 3\frac{1}{2}$       (vii)  $8\frac{1}{2} - 3\frac{5}{8}$

2. Arrange the following in descending order:

- (i)  $\frac{2}{9}, \frac{2}{3}, \frac{8}{21}$       (ii)  $\frac{1}{5}, \frac{3}{7}, \frac{7}{10}$

3. In a “magic square”, the sum of the numbers in each row, in each column and along the diagonals is the same. Is this a magic square?

$\frac{4}{11}$	$\frac{9}{11}$	$\frac{2}{11}$
$\frac{3}{11}$	$\frac{5}{11}$	$\frac{7}{11}$
$\frac{8}{11}$	$\frac{1}{11}$	$\frac{6}{11}$

(Along the first row  $\frac{4}{11} + \frac{9}{11} + \frac{2}{11} = \frac{15}{11}$ ).

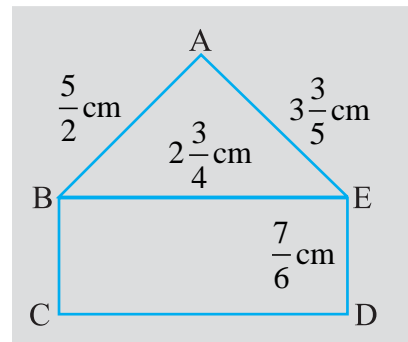


4. A rectangular sheet of paper is  $12\frac{1}{2}$  cm long and  $10\frac{2}{3}$  cm wide.

Find its perimeter.

5. Find the perimeters of (i)  $\triangle ABE$  (ii) the rectangle BCDE in this figure. Whose perimeter is greater?

6. Salil wants to put a picture in a frame. The picture is  $7\frac{3}{5}$  cm wide.



To fit in the frame the picture cannot be more than  $7\frac{3}{10}$  cm wide. How much should the picture be trimmed?

7. Ritu ate  $\frac{3}{5}$  part of an apple and the remaining apple was eaten by her brother Somu. How much part of the apple did Somu eat? Who had the larger share? By how much?
8. Michael finished colouring a picture in  $\frac{7}{12}$  hour. Vaibhav finished colouring the same picture in  $\frac{3}{4}$  hour. Who worked longer? By what fraction was it longer?

## 2.3 MULTIPLICATION OF FRACTIONS

You know how to find the area of a rectangle. It is equal to length  $\times$  breadth. If the length and breadth of a rectangle are 7 cm and 4 cm respectively, then what will be its area? Its area would be  $7 \times 4 = 28 \text{ cm}^2$ .

What will be the area of the rectangle if its length and breadth are  $7\frac{1}{2}$  cm and  $3\frac{1}{2}$  cm respectively? You will say it will be  $7\frac{1}{2} \times 3\frac{1}{2} = \frac{15}{2} \times \frac{7}{2} \text{ cm}^2$ . The numbers  $\frac{15}{2}$  and  $\frac{7}{2}$  are fractions. To calculate the area of the given rectangle, we need to know how to multiply fractions. We shall learn that now.

### 2.3.1 Multiplication of a Fraction by a Whole Number

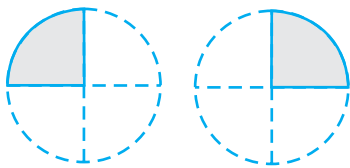


Fig 2.1

Observe the pictures at the left (Fig 2.1). Each shaded part is  $\frac{1}{4}$  part of a circle. How much will the two shaded parts represent together? They will represent  $\frac{1}{4} + \frac{1}{4} = 2 \times \frac{1}{4}$

Combining the two shaded parts, we get Fig 2.2. What part of a circle does the shaded part in Fig 2.2 represent? It represents  $\frac{2}{4}$  part of a circle.

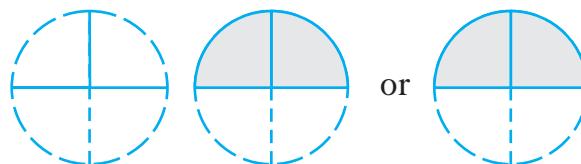


Fig 2.2

The shaded portions in Fig 2.1 taken together are the same as the shaded portion in Fig 2.2, i.e., we get Fig 2.3.



Fig 2.3

or  $2 \times \frac{1}{4} = \frac{2}{4}$ .

Can you now tell what this picture will represent? (Fig 2.4)

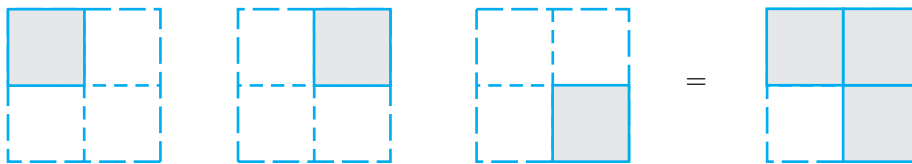


Fig 2.4

And this? (Fig 2.5)

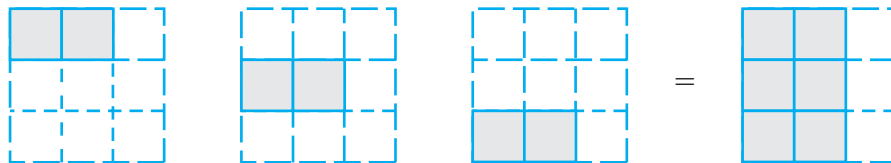


Fig 2.5

Let us now find  $3 \times \frac{1}{2}$ .

We have  $3 \times \frac{1}{2} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = \frac{3}{2}$

We also have  $\frac{1}{2} + \frac{1}{2} + \frac{1}{2} = \frac{1+1+1}{2} = \frac{3 \times 1}{2} = \frac{3}{2}$

So  $3 \times \frac{1}{2} = \frac{3 \times 1}{2} = \frac{3}{2}$

Similarly  $\frac{2}{3} \times 5 = \frac{2 \times 5}{3} = ?$

Can you tell  $3 \times \frac{2}{7} = ?$       $4 \times \frac{3}{5} = ?$

The fractions that we considered till now, i.e.,  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{2}{7}$  and  $\frac{3}{5}$  were proper fractions.

For improper fractions also we have,

$$2 \times \frac{5}{3} = \frac{2 \times 5}{3} = \frac{10}{3}$$

Try,  $3 \times \frac{8}{7} = ?$   $4 \times \frac{7}{5} = ?$

Thus, to multiply a whole number with a proper or an improper fraction, we multiply the whole number with the numerator of the fraction, keeping the denominator same.

### TRY THESE



1. Find: (a)  $\frac{2}{7} \times 3$       (b)  $\frac{9}{7} \times 6$       (c)  $3 \times \frac{1}{8}$       (d)  $\frac{13}{11} \times 6$

If the product is an improper fraction express it as a mixed fraction.

2. Represent pictorially:  $2 \frac{2}{5} = \frac{4}{5}$

### TRY THESE

Find: (i)  $5 \times 2\frac{3}{7}$

(ii)  $1\frac{4}{9} \times 6$



To multiply a mixed fraction to a whole number, first convert the mixed fraction to an improper fraction and then multiply.

Therefore,  $3 \times 2\frac{5}{7} = 3 \times \frac{19}{7} = \frac{57}{7} = 8\frac{1}{7}$ .

Similarly,  $2 \times 4\frac{2}{5} = 2 \times \frac{22}{5} = ?$



### Fraction as an operator 'of'

Observe these figures (Fig 2.6)

The two squares are exactly similar.

Each shaded portion represents  $\frac{1}{2}$  of 1.

So, both the shaded portions together will represent  $\frac{1}{2}$  of 2.

Combine the 2 shaded  $\frac{1}{2}$  parts. It represents 1.

So, we say  $\frac{1}{2}$  of 2 is 1. We can also get it as  $\frac{1}{2} \times 2 = 1$ .

Thus,  $\frac{1}{2}$  of 2 =  $\frac{1}{2} \times 2 = 1$

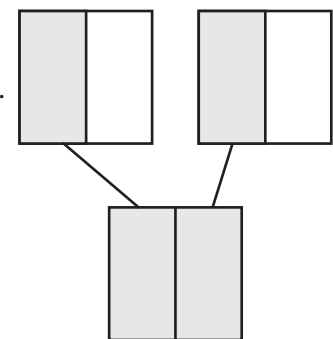


Fig 2.6

Also, look at these similar squares (Fig 2.7).

Each shaded portion represents  $\frac{1}{2}$  of 1.

So, the three shaded portions represent  $\frac{1}{2}$  of 3.

Combine the 3 shaded parts.

It represents  $1\frac{1}{2}$  i.e.,  $\frac{3}{2}$ .

So,  $\frac{1}{2}$  of 3 is  $\frac{3}{2}$ . Also,  $\frac{1}{2} \times 3 = \frac{3}{2}$ .

Thus,  $\frac{1}{2}$  of 3 =  $\frac{1}{2} \times 3 = \frac{3}{2}$ .

So we see that ‘of’ represents multiplication.

Farida has 20 marbles. Reshma has  $\frac{1}{5}$ th of the number of marbles what Farida has. How many marbles Reshma has? As, ‘of’ indicates multiplication, so, Reshma has  $\frac{1}{5} \times 20 = 4$  marbles.

Similarly, we have  $\frac{1}{2}$  of 16 is  $\frac{1}{2} \times 16 = \frac{16}{2} = 8$ .

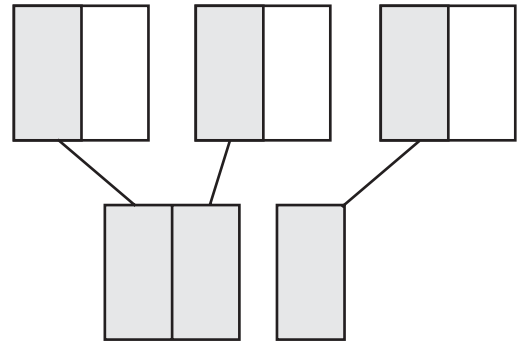


Fig 2.7



### TRY THESE

Can you tell, what is (i)  $\frac{1}{2}$  of 10?, (ii)  $\frac{1}{4}$  of 16?, (iii)  $\frac{2}{5}$  of 25?

**EXAMPLE 5** In a class of 40 students  $\frac{1}{5}$  of the total number of students like to study English,  $\frac{2}{5}$  of the total number like to study Mathematics and the remaining students like to study Science.

- How many students like to study English?
- How many students like to study Mathematics?
- What fraction of the total number of students like to study Science?

**SOLUTION** Total number of students in the class = 40.

- Of these  $\frac{1}{5}$  of the total number of students like to study English.



Thus, the number of students who like to study English =  $\frac{1}{5}$  of  $40 = \frac{1}{5} \times 40 = 8$ .

(ii) Try yourself.

(iii) The number of students who like English and Mathematics =  $8 + 16 = 24$ . Thus, the number of students who like Science =  $40 - 24 = 16$ .

Thus, the required fraction is  $\frac{16}{40}$ .

## EXERCISE 2.2

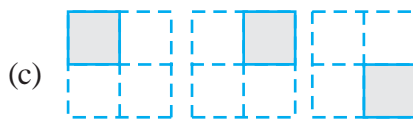
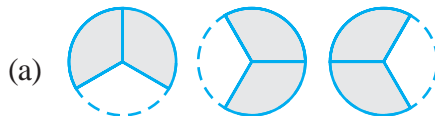
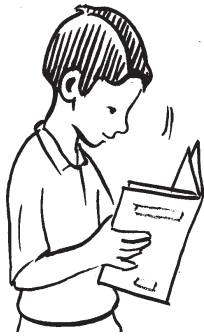
1. Which of the drawings (a) to (d) show :

(i)  $2 \times \frac{1}{5}$

(ii)  $2 \times \frac{1}{2}$

(iii)  $3 \times \frac{2}{3}$

(iv)  $3 \times \frac{1}{4}$

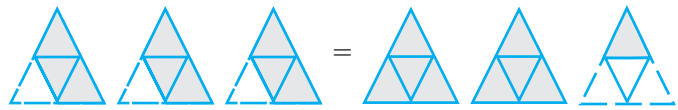
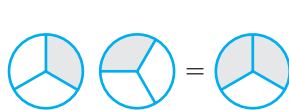


2. Some pictures (a) to (c) are given below. Tell which of them show:

(i)  $3 \times \frac{1}{5} = \frac{3}{5}$

(ii)  $2 \times \frac{1}{3} = \frac{2}{3}$

(iii)  $3 \times \frac{3}{4} = 2\frac{1}{4}$



(a)

(b)



(c)

3. Multiply and reduce to lowest form and convert into a mixed fraction:

(i)  $7 \times \frac{3}{5}$

(ii)  $4 \times \frac{1}{3}$

(iii)  $2 \times \frac{6}{7}$

(iv)  $5 \times \frac{2}{9}$

(v)  $\frac{2}{3} \times 4$

(vi)  $\frac{5}{2} \times 6$

(vii)  $11 \times \frac{4}{7}$

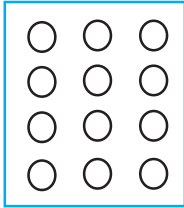
(viii)  $20 \times \frac{4}{5}$

(ix)  $13 \times \frac{1}{3}$

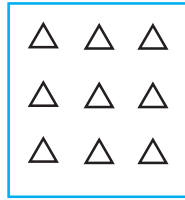
(x)  $15 \times \frac{3}{5}$



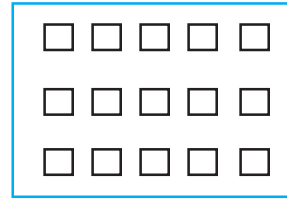
4. Shade: (i)  $\frac{1}{2}$  of the circles in box (a) (ii)  $\frac{2}{3}$  of the triangles in box (b)  
 (iii)  $\frac{3}{5}$  of the squares in box (c).



(a)



(b)



(c)

5. Find:

- (a)  $\frac{1}{2}$  of (i) 24 (ii) 46 (b)  $\frac{2}{3}$  of (i) 18 (ii) 27  
 (c)  $\frac{3}{4}$  of (i) 16 (ii) 36 (d)  $\frac{4}{5}$  of (i) 20 (ii) 35

6. Multiply and express as a mixed fraction :

- (a)  $3 \times 5\frac{1}{5}$  (b)  $5 \times 6\frac{3}{4}$  (c)  $7 \times 2\frac{1}{4}$   
 (d)  $4 \times 6\frac{1}{3}$  (e)  $3\frac{1}{4} \times 6$  (f)  $3\frac{2}{5} \times 8$

7. Find: (a)  $\frac{1}{2}$  of (i)  $2\frac{3}{4}$  (ii)  $4\frac{2}{9}$  (b)  $\frac{5}{8}$  of (i)  $3\frac{5}{6}$  (ii)  $9\frac{2}{3}$

8. Vidya and Pratap went for a picnic. Their mother gave them a water bottle that contained 5 litres of water. Vidya consumed  $\frac{2}{5}$  of the water. Pratap consumed the remaining water.

- (i) How much water did Vidya drink?  
 (ii) What fraction of the total quantity of water did Pratap drink?



### 2.3.2 Multiplication of a Fraction by a Fraction

Farida had a 9 cm long strip of ribbon. She cut this strip into four equal parts. How did she do it? She folded the strip twice. What fraction of the total length will each part represent?

Each part will be  $\frac{9}{4}$  of the strip. She took one part and divided it in two equal parts by

folding the part once. What will one of the pieces represent? It will represent  $\frac{1}{2}$  of  $\frac{9}{4}$  or

$$\frac{1}{2} \times \frac{9}{4}.$$

Let us now see how to find the product of two fractions like  $\frac{1}{2} \times \frac{9}{4}$ .

To do this we first learn to find the products like  $\frac{1}{2} \times \frac{1}{3}$ .



Fig 2.8

- (a) How do we find  $\frac{1}{3}$  of a whole? We divide the whole in three equal parts. Each of the three parts represents  $\frac{1}{3}$  of the whole. Take one part of these three parts, and shade it as shown in Fig 2.8.

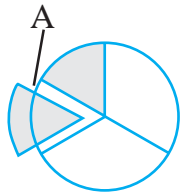


Fig 2.9

- (b) How will you find  $\frac{1}{2}$  of this shaded part? Divide this one-third ( $\frac{1}{3}$ ) shaded part into two equal parts. Each of these two parts represents  $\frac{1}{2}$  of  $\frac{1}{3}$  i.e.,  $\frac{1}{2} \times \frac{1}{3}$  (Fig 2.9).

Take out 1 part of these two and name it 'A'. 'A' represents  $\frac{1}{2} \times \frac{1}{3}$ .

- (c) What fraction is 'A' of the whole? For this, divide each of the remaining  $\frac{1}{3}$  parts also in two equal parts. How many such equal parts do you have now? There are six such equal parts. 'A' is one of these parts.

So, 'A' is  $\frac{1}{6}$  of the whole. Thus,  $\frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$ .

How did we decide that 'A' was  $\frac{1}{6}$  of the whole? The whole was divided in  $6 = 2 \times 3$  parts and  $1 = 1 \times 1$  part was taken out of it.

Thus, 
$$\frac{1}{2} \times \frac{1}{3} = \frac{1}{6} = \frac{1 \times 1}{2 \times 3}$$

or 
$$\frac{1}{2} \times \frac{1}{3} = \frac{1 \times 1}{2 \times 3}$$

The value of  $\frac{1}{3} \times \frac{1}{2}$  can be found in a similar way. Divide the whole into two equal parts and then divide one of these parts in three equal parts. Take one of these parts. This will represent  $\frac{1}{3} \times \frac{1}{2}$  i.e.,  $\frac{1}{6}$ .

Therefore  $\frac{1}{3} \times \frac{1}{2} = \frac{1}{6} = \frac{1 \times 1}{3 \times 2}$  as discussed earlier.

Hence  $\frac{1}{2} \times \frac{1}{3} = \frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$

Find  $\frac{1}{3} \times \frac{1}{4}$  and  $\frac{1}{4} \times \frac{1}{3}$ ;  $\frac{1}{2} \times \frac{1}{5}$  and  $\frac{1}{5} \times \frac{1}{2}$  and check whether you get

$$\frac{1}{3} \times \frac{1}{4} = \frac{1}{4} \times \frac{1}{3}; \quad \frac{1}{2} \times \frac{1}{5} = \frac{1}{5} \times \frac{1}{2}$$

### TRY THESE

Fill in these boxes:

(i)  $\frac{1}{2} \times \frac{1}{7} = \frac{1 \times 1}{2 \times 7} = \square$

(ii)  $\frac{1}{5} \times \frac{1}{7} = \square = \square$

(iii)  $\frac{1}{7} \times \frac{1}{2} = \square = \square$

(iv)  $\frac{1}{7} \times \frac{1}{5} = \square = \square$



**EXAMPLE 6** Sushant reads  $\frac{1}{3}$  part of a book in 1 hour. How much part of the book will he read in  $2\frac{1}{5}$  hours?

**SOLUTION** The part of the book read by Sushant in 1 hour =  $\frac{1}{3}$ .

So, the part of the book read by him in  $2\frac{1}{5}$  hours =  $2\frac{1}{5} \times \frac{1}{3}$   
 $= \frac{11}{5} \times \frac{1}{3} = \frac{11}{5} \times \frac{1}{3} = \frac{11}{15}$

Let us now find  $\frac{1}{2} \times \frac{5}{3}$ . We know that  $\frac{5}{3} = \frac{1}{3} \times 5$ .

$$\text{So, } \frac{1}{2} \times \frac{5}{3} = \frac{1}{2} \times \frac{1}{3} \times 5 = \frac{1}{6} \times 5 = \frac{5}{6}$$



Also,  $\frac{5}{6} = \frac{1 \times 5}{2 \times 3}$ . Thus,  $\frac{1}{2} \times \frac{5}{3} = \frac{1 \times 5}{2 \times 3} = \frac{5}{6}$ .

This is also shown by the figures drawn below. Each of these five equal shapes (Fig 2.10) are parts of five similar circles. Take one such shape. To obtain this shape we first divide a circle in three equal parts. Further divide each of these three parts in two equal parts. One part out of it is the shape we considered. What will it represent?

It will represent  $\frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$ . The total of such parts would be  $5 \times \frac{1}{6} = \frac{5}{6}$ .



Fig 2.10

### TRY THESE



Find:  $\frac{1}{3} \times \frac{4}{5}$ ;  $\frac{2}{3} \times \frac{1}{5}$

Similarly  $\frac{3}{5} \times \frac{1}{7} = \frac{3 \times 1}{5 \times 7} = \frac{3}{35}$ .

We can thus find  $\frac{2}{3} \times \frac{7}{5}$  as  $\frac{2}{3} \times \frac{7}{5} = \frac{2 \times 7}{3 \times 5} = \frac{14}{15}$ .

So, we find that we multiply two fractions as  $\frac{\text{Product of Numerators}}{\text{Product of Denominators}}$ .

### Value of the Products

### TRY THESE

Find:  $\frac{8}{3} \times \frac{4}{7}$ ;  $\frac{3}{4} \times \frac{2}{3}$ .

You have seen that the product of two whole numbers is bigger than each of the two whole numbers. For example,  $3 \times 4 = 12$  and  $12 > 4$ ,  $12 > 3$ . What happens to the value of the product when we multiply two fractions?

Let us first consider the product of two proper fractions.

We have,

$\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$	$\frac{8}{15} < \frac{2}{3}, \frac{8}{15} < \frac{4}{5}$	Product is less than each of the fractions
$\frac{1}{5} \times \frac{2}{7} = \dots\dots\dots$	$\dots\dots\dots, \dots\dots\dots$	$\dots\dots\dots$
$\frac{3}{5} \times \frac{\square}{8} = \dots\dots\dots$	$\dots\dots\dots, \dots\dots\dots$	$\dots\dots\dots$
$\frac{2}{\square} \times \frac{4}{9} = \frac{8}{45}$	$\dots\dots\dots, \dots\dots\dots$	$\dots\dots\dots$

You will find that *when two proper fractions are multiplied, the product is less than each of the fractions. Or, we say the value of the product of two proper fractions is smaller than each of the two fractions.*

Check this by constructing five more examples.

Let us now multiply two improper fractions.

$\frac{7}{3} \times \frac{5}{2} = \frac{35}{6}$	$\frac{35}{6} > \frac{7}{3}, \frac{35}{6} > \frac{5}{2}$	Product is greater than each of the fractions
$\frac{6}{5} \times \frac{\square}{3} = \frac{24}{15}$	-----,-----	-----
	-----,-----	-----
$\frac{3}{\square} \times \frac{8}{7} = \frac{24}{14}$	-----,-----	-----

We find that *the product of two improper fractions is greater than each of the two fractions.*

$\frac{9}{2} \times \frac{7}{\square} = \frac{63}{8}$  Or, *the value of the product of two improper fractions is more than each of the two fractions.*

Construct five more examples for yourself and verify the above statement.

Let us now multiply a proper and an improper fraction, say  $\frac{2}{3}$  and  $\frac{7}{5}$ .

We have  $\frac{2}{3} \times \frac{7}{5} = \frac{14}{15}$ . Here,  $\frac{14}{15} < \frac{7}{5}$  and  $\frac{14}{15} > \frac{2}{3}$

The product obtained is less than the improper fraction and greater than the proper fraction involved in the multiplication.

Check it for  $\frac{6}{5} \times \frac{2}{7}, \frac{8}{3} \times \frac{4}{5}$ .

### EXERCISE 2.3

1. Find:

(i)  $\frac{1}{4}$  of (a)  $\frac{1}{4}$  (b)  $\frac{3}{5}$  (c)  $\frac{4}{3}$

(ii)  $\frac{1}{7}$  of (a)  $\frac{2}{9}$  (b)  $\frac{6}{5}$  (c)  $\frac{3}{10}$



2. Multiply and reduce to lowest form (if possible) :

$$\begin{array}{llll} \text{(i)} \quad \frac{2}{3} \times 2\frac{2}{3} & \text{(ii)} \quad \frac{2}{7} \times \frac{7}{9} & \text{(iii)} \quad \frac{3}{8} \times \frac{6}{4} & \text{(iv)} \quad \frac{9}{5} \times \frac{3}{5} \\ \text{(v)} \quad \frac{1}{3} \times \frac{15}{8} & \text{(vi)} \quad \frac{11}{2} \times \frac{3}{10} & \text{(vii)} \quad \frac{4}{5} \times \frac{12}{7} & \end{array}$$

3. Multiply the following fractions:

$$\begin{array}{llll} \text{(i)} \quad \frac{2}{5} \times 5\frac{1}{4} & \text{(ii)} \quad 6\frac{2}{5} \times \frac{7}{9} & \text{(iii)} \quad \frac{3}{2} \times 5\frac{1}{3} & \text{(iv)} \quad \frac{5}{6} \times 2\frac{3}{7} \\ \text{(v)} \quad 3\frac{2}{5} \times \frac{4}{7} & \text{(vi)} \quad 2\frac{3}{5} \times 3 & \text{(vii)} \quad 3\frac{4}{7} \times \frac{3}{5} & \end{array}$$

4. Which is greater:

$$\text{(i)} \quad \frac{2}{7} \text{ of } \frac{3}{4} \quad \text{or} \quad \frac{3}{5} \text{ of } \frac{5}{8} \quad \text{(ii)} \quad \frac{1}{2} \text{ of } \frac{6}{7} \quad \text{or} \quad \frac{2}{3} \text{ of } \frac{3}{7}$$

5. Saili plants 4 saplings, in a row, in her garden. The distance between two adjacent saplings is  $\frac{3}{4}$  m. Find the distance between the first and the last sapling.

6. Lipika reads a book for  $1\frac{3}{4}$  hours everyday. She reads the entire book in 6 days. How many hours in all were required by her to read the book?

7. A car runs 16 km using 1 litre of petrol. How much distance will it cover using  $2\frac{3}{4}$  litres of petrol.

8. (a) (i) Provide the number in the box  $\square$ , such that  $\frac{2}{3} \times \square = \frac{10}{30}$ .

(ii) The simplest form of the number obtained in  $\square$  is \_\_\_\_\_.

(b) (i) Provide the number in the box  $\square$ , such that  $\frac{3}{5} \times \square = \frac{24}{75}$ .

(ii) The simplest form of the number obtained in  $\square$  is \_\_\_\_\_.



## 2.4 DIVISION OF FRACTIONS

John has a paper strip of length 6 cm. He cuts this strip in smaller strips of length 2 cm each. You know that he would get  $6 \div 2 = 3$  strips.

John cuts another strip of length 6 cm into smaller strips of length  $\frac{3}{2}$  cm each. How many strips will he get now? He will get  $6 \div \frac{3}{2}$  strips.

A paper strip of length  $\frac{15}{2}$  cm can be cut into smaller strips of length  $\frac{3}{2}$  cm each to give  $\frac{15}{2} \div \frac{3}{2}$  pieces.

So, we are required to divide a whole number by a fraction or a fraction by another fraction. Let us see how to do that.

### 2.4.1 Division of Whole Number by a Fraction

Let us find  $1 \div \frac{1}{2}$ .

We divide a whole into a number of equal parts such that each part is half of the whole.

The number of such half ( $\frac{1}{2}$ ) parts would be  $1 \div \frac{1}{2}$ . Observe the figure (Fig 2.11). How many half parts do you see?

There are two half parts.

So,  $1 \div \frac{1}{2} = 2$ . Also,  $1 \times \frac{2}{1} = 1 \times 2 = 2$ .

Thus,  $1 \div \frac{1}{2} = 1 \times \frac{2}{1}$

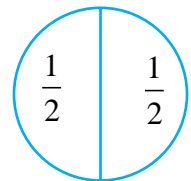


Fig 2.11

Similarly,  $3 \div \frac{1}{4} =$  number of  $\frac{1}{4}$  parts obtained when each of the 3 whole, are divided

into  $\frac{1}{4}$  equal parts = 12 (From Fig 2.12)

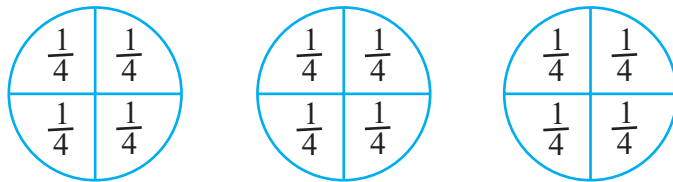


Fig 2.12

Observe also that,  $3 \times \frac{4}{1} = 3 \times 4 = 12$ . Thus,  $3 \div \frac{1}{4} = 3 \times \frac{4}{1} = 12$ .

Find in a similar way,  $3 \div \frac{1}{2}$  and  $3 \times \frac{2}{1}$ .



### Reciprocal of a fraction

The number  $\frac{2}{1}$  can be obtained by interchanging the numerator and denominator of

$\frac{1}{2}$  or by inverting  $\frac{1}{2}$ . Similarly,  $\frac{3}{1}$  is obtained by inverting  $\frac{1}{3}$ .

Let us first see about the inverting of such numbers.

Observe these products and fill in the blanks :

$7 \times \frac{1}{7} = 1$	$\frac{5}{4} \times \frac{4}{5} = \text{-----}$
$\frac{1}{9} \times 9 = \text{-----}$	$\frac{2}{7} \times \text{-----} = 1$
$\frac{2}{3} \times \frac{3}{2} = \frac{2 \times 3}{3 \times 2} = \frac{6}{6} = 1$	$\text{-----} \times \frac{5}{9} = 1$

Multiply five more such pairs.

**The non-zero numbers whose product with each other is 1, are called the reciprocals of each other.** So reciprocal of  $\frac{5}{9}$  is  $\frac{9}{5}$  and the reciprocal of  $\frac{9}{5}$  is  $\frac{5}{9}$ . What

is the reciprocal of  $\frac{1}{9}$ ?  $\frac{2}{7}$ ?

You will see that the reciprocal of  $\frac{2}{3}$  is obtained by inverting it. You get  $\frac{3}{2}$ .

### THINK, DISCUSS AND WRITE



- Will the reciprocal of a proper fraction be again a proper fraction?
- Will the reciprocal of an improper fraction be again an improper fraction?

Therefore, we can say that

$$1 \div \frac{1}{2} = 1 \times \frac{2}{1} = 1 \times \text{reciprocal of } \frac{1}{2}.$$

$$3 \div \frac{1}{4} = 3 \times \frac{4}{1} = 3 \times \text{reciprocal of } \frac{1}{4}.$$

$$3 \div \frac{1}{2} = \text{-----} = \text{-----}.$$

$$\text{So, } 2 \div \frac{3}{4} = 2 \times \text{reciprocal of } \frac{3}{4} = 2 \times \frac{4}{3}.$$

$$5 \div \frac{2}{9} = 5 \times \text{-----} = 5 \times \text{-----}$$





Thus, to divide a whole number by any fraction, multiply that whole number by the reciprocal of that fraction.

**TRY THESE**

Find: (i)  $7 \div \frac{2}{5}$       (ii)  $6 \div \frac{4}{7}$       (iii)  $2 \div \frac{8}{9}$



- While dividing a whole number by a mixed fraction, first convert the mixed fraction into improper fraction and then solve it.

Thus,  $4 \div 2\frac{2}{5} = 4 \div \frac{12}{5} = ?$       Also,  $5 \div 3\frac{1}{3} = 5 \div \frac{10}{3} = ?$

**TRY THESE**

Find: (i)  $6 \div 5\frac{1}{3}$   
(ii)  $7 \div 2\frac{4}{7}$

**2.4.2 Division of a Fraction by a Whole Number**

- What will be  $\frac{3}{4} \div 3$ ?

Based on our earlier observations we have:  $\frac{3}{4} \div 3 = \frac{3}{4} \div \frac{3}{1} = \frac{3}{4} \times \frac{1}{3} = \frac{3}{12} = \frac{1}{4}$

So,  $\frac{2}{3} \div 7 = \frac{2}{3} \times \frac{1}{7} = ?$       What is  $\frac{5}{7} \div 6$ ,  $\frac{2}{7} \div 8$ ?

- While dividing mixed fractions by whole numbers, convert the mixed fractions into improper fractions. That is,

$2\frac{2}{3} \div 5 = \frac{8}{3} \div 5 = \dots\dots$ ;  $4\frac{2}{5} \div 3 = \dots\dots = \dots\dots$ ;  $2\frac{3}{5} \div 2 = \dots\dots = \dots\dots$

**2.4.3 Division of a Fraction by Another Fraction**

We can now find  $\frac{1}{3} \div \frac{6}{5}$ .

$\frac{1}{3} \div \frac{6}{5} = \frac{1}{3} \times$  reciprocal of  $\frac{6}{5} = \frac{1}{3} \times \frac{5}{6} = \frac{5}{18}$ .

Similarly,  $\frac{8}{5} \div \frac{2}{3} = \frac{8}{5} \times$  reciprocal of  $\frac{2}{3} = ?$       and,  $\frac{1}{2} \div \frac{3}{4} = ?$

**TRY THESE**

Find: (i)  $\frac{3}{5} \div \frac{1}{2}$       (ii)  $\frac{1}{2} \div \frac{3}{5}$       (iii)  $2\frac{1}{2} \div \frac{3}{5}$       (iv)  $5\frac{1}{6} \div \frac{9}{2}$



### EXERCISE 2.4

1. Find:

(i)  $12 \div \frac{3}{4}$

(ii)  $14 \div \frac{5}{6}$

(iii)  $8 \div \frac{7}{3}$

(iv)  $4 \div \frac{8}{3}$

(v)  $3 \div 2\frac{1}{3}$

(vi)  $5 \div 3\frac{4}{7}$

2. Find the reciprocal of each of the following fractions. Classify the reciprocals as proper fractions, improper fractions and whole numbers.

(i)  $\frac{3}{7}$

(ii)  $\frac{5}{8}$

(iii)  $\frac{9}{7}$

(iv)  $\frac{6}{5}$

(v)  $\frac{12}{7}$

(vi)  $\frac{1}{8}$

(vii)  $\frac{1}{11}$

3. Find:

(i)  $\frac{7}{3} \div 2$

(ii)  $\frac{4}{9} \div 5$

(iii)  $\frac{6}{13} \div 7$

(iv)  $4\frac{1}{3} \div 3$

(v)  $3\frac{1}{2} \div 4$

(vi)  $4\frac{3}{7} \div 7$

4. Find:

(i)  $\frac{2}{5} \div \frac{1}{2}$

(ii)  $\frac{4}{9} \div \frac{2}{3}$

(iii)  $\frac{3}{7} \div \frac{8}{7}$

(iv)  $2\frac{1}{3} \div \frac{3}{5}$

(v)  $3\frac{1}{2} \div \frac{8}{3}$

(vi)  $\frac{2}{5} \div 1\frac{1}{2}$

(vii)  $3\frac{1}{5} \div 1\frac{2}{3}$

(viii)  $2\frac{1}{5} \div 1\frac{1}{5}$

## 2.5 HOW WELL HAVE YOU LEARNT ABOUT DECIMAL NUMBERS

You have learnt about decimal numbers in the earlier classes. Let us briefly recall them here. Look at the following table and fill up the blank spaces.

Hundreds	Tens	Ones	Tenths	Hundredths	Thousandths	Number
(100)	(10)	(1)	$\left(\frac{1}{10}\right)$	$\left(\frac{1}{100}\right)$	$\left(\frac{1}{1000}\right)$	
2	5	3	1	4	7	253.147
6	2	9	3	2	1	.....
0	4	3	1	9	2	.....
.....	1	4	2	5	1	514.251
2	.....	6	5	1	2	236.512
.....	2	.....	5	.....	3	724.503
6	.....	4	.....	2	.....	614.326
0	1	0	5	3	0	.....

In the table, you wrote the decimal number, given its place-value expansion. You can do the reverse, too. That is, given the number you can write its expanded form. For

example,  $253.417 = 2 \times 100 + 5 \times 10 + 3 \times 1 + 4 \times \left(\frac{1}{10}\right) + 1 \times \left(\frac{1}{100}\right) + 7 \times \left(\frac{1}{1000}\right)$ .

John has ₹ 15.50 and Salma has ₹ 15.75. Who has more money? To find this we need to compare the decimal numbers 15.50 and 15.75. To do this, we first compare the digits on the left of the decimal point, starting from the leftmost digit. Here both the digits 1 and 5, to the left of the decimal point, are same. So we compare the digits on the right of the decimal point starting from the tenths place. We find that  $5 < 7$ , so we say  $15.50 < 15.75$ . Thus, Salma has more money than John.

If the digits at the tenths place are also same then compare the digits at the hundredths place and so on.

Now compare quickly, 35.63 and 35.67; 20.1 and 20.01; 19.36 and 29.36.

While converting lower units of money, length and weight, to their higher units, we are required to use decimals. For example, 3 paise = ₹  $\frac{3}{100}$  = ₹ 0.03, 5g =  $\frac{5}{1000}$  kg = 0.005 kg, 7 cm = 0.07 m.

Write 75 paise = ₹ \_\_\_\_\_, 250 g = \_\_\_\_\_ kg, 85 cm = \_\_\_\_\_ m.

We also know how to add and subtract decimals. Thus,  $21.36 + 37.35$  is

$$\begin{array}{r} 21.36 \\ + 37.35 \\ \hline 58.71 \end{array}$$

What is the value of  $0.19 + 2.3$  ?

The difference  $29.35 - 4.56$  is

$$\begin{array}{r} 29.35 \\ - 04.56 \\ \hline 24.79 \end{array}$$

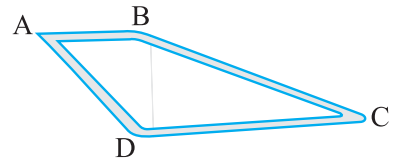
Tell the value of  $39.87 - 21.98$ .

## EXERCISE 2.5

- Which is greater?
  - 0.5 or 0.05
  - 0.7 or 0.5
  - 7 or 0.7
  - 1.37 or 1.49
  - 2.03 or 2.30
  - 0.8 or 0.88.
- Express as rupees using decimals :
  - 7 paise
  - 7 rupees 7 paise
  - 77 rupees 77 paise
  - 50 paise
  - 235 paise.
- Express 5 cm in metre and kilometre
  - Express 35 mm in cm, m and km



4. Express in kg:
- (i) 200 g            (ii) 3470 g            (iii) 4 kg 8 g
5. Write the following decimal numbers in the expanded form:
- (i) 20.03            (ii) 2.03            (iii) 200.03            (iv) 2.034
6. Write the place value of 2 in the following decimal numbers:
- (i) 2.56            (ii) 21.37            (iii) 10.25            (iv) 9.42            (v) 63.352.
7. Dinesh went from place A to place B and from there to place C. A is 7.5 km from B and B is 12.7 km from C. Ayub went from place A to place D and from there to place C. D is 9.3 km from A and C is 11.8 km from D. Who travelled more and by how much?
8. Shyama bought 5 kg 300 g apples and 3 kg 250 g mangoes. Sarala bought 4 kg 800 g oranges and 4 kg 150 g bananas. Who bought more fruits?
9. How much less is 28 km than 42.6 km?



## 2.6 MULTIPLICATION OF DECIMAL NUMBERS

Reshma purchased 1.5kg vegetable at the rate of ₹ 8.50 per kg. How much money should she pay? Certainly it would be ₹  $(8.50 \times 1.50)$ . Both 8.5 and 1.5 are decimal numbers. So, we have come across a situation where we need to know how to multiply two decimals. Let us now learn the multiplication of two decimal numbers.

First we find  $0.1 \times 0.1$ .

$$\text{Now, } 0.1 = \frac{1}{10}. \text{ So, } 0.1 \times 0.1 = \frac{1}{10} \times \frac{1}{10} = \frac{1 \times 1}{10 \times 10} = \frac{1}{100} = 0.01.$$

Let us see its pictorial representation (Fig 2.13)

The fraction  $\frac{1}{10}$  represents 1 part out of 10 equal parts.

The shaded part in the picture represents  $\frac{1}{10}$ .

We know that,

$$\frac{1}{10} \times \frac{1}{10} \text{ means } \frac{1}{10} \text{ of } \frac{1}{10}. \text{ So, divide this}$$

$\frac{1}{10}$ <sup>th</sup> part into 10 equal parts and take one part out of it.

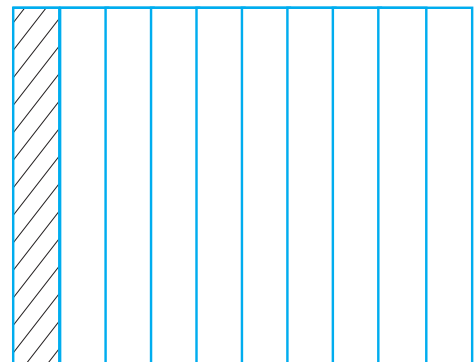


Fig 2.13

Thus, we have, (Fig 2.14).

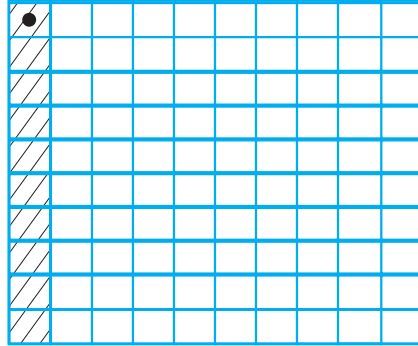


Fig 2.14



The dotted square is one part out of 10 of the  $\frac{1}{10}$ <sup>th</sup> part. That is, it represents

$$\frac{1}{10} \times \frac{1}{10} \text{ or } 0.1 \times 0.1.$$

Can the dotted square be represented in some other way?

How many small squares do you find in Fig 2.14?

There are 100 small squares. So the dotted square represents one out of 100 or 0.01.

Hence,  $0.1 \times 0.1 = 0.01$ .

Note that 0.1 occurs two times in the product. In 0.1 there is one digit to the right of the decimal point. In 0.01 there are two digits (i.e., 1 + 1) to the right of the decimal point.

Let us now find  $0.2 \times 0.3$ .

$$\text{We have, } 0.2 \times 0.3 = \frac{2}{10} \times \frac{3}{10}$$

As we did for  $\frac{1}{10} \times \frac{1}{10}$ , let us divide the square into 10

equal parts and take three parts out of it, to get  $\frac{3}{10}$ . Again

divide each of these three equal parts into 10 equal parts and

take two from each. We get  $\frac{2}{10} \times \frac{3}{10}$ .

The dotted squares represent  $\frac{2}{10} \times \frac{3}{10}$  or  $0.2 \times 0.3$ . (Fig 2.15)

Since there are 6 dotted squares out of 100, so they also represent 0.06.

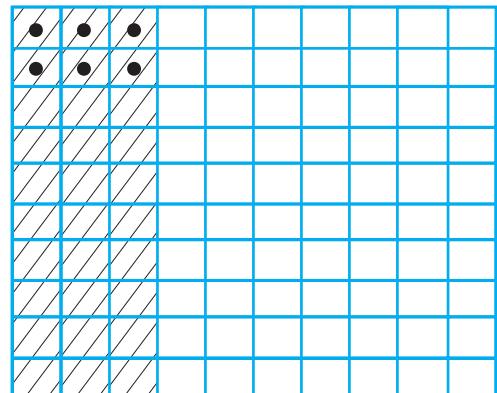


Fig 2.15

Thus,  $0.2 \times 0.3 = 0.06$ .

Observe that  $2 \times 3 = 6$  and the number of digits to the right of the decimal point in  $0.06$  is  $2 (= 1 + 1)$ .

Check whether this applies to  $0.1 \times 0.1$  also.

Find  $0.2 \times 0.4$  by applying these observations.

While finding  $0.1 \times 0.1$  and  $0.2 \times 0.3$ , you might have noticed that first we multiplied them as whole numbers ignoring the decimal point. In  $0.1 \times 0.1$ , we found  $01 \times 01$  or  $1 \times 1$ . Similarly in  $0.2 \times 0.3$  we found  $02 \times 03$  or  $2 \times 3$ .

Then, we counted the number of digits starting from the rightmost digit and moved towards left. We then put the decimal point there. The number of digits to be counted is obtained by adding the number of digits to the right of the decimal point in the decimal numbers that are being multiplied.

Let us now find  $1.2 \times 2.5$ .

Multiply 12 and 25. We get 300. Both, in 1.2 and 2.5, there is 1 digit to the right of the decimal point. So, count  $1 + 1 = 2$  digits from the rightmost digit (i.e., 0) in 300 and move towards left. We get 3.00 or 3.

Find in a similar way  $1.5 \times 1.6$ ,  $2.4 \times 4.2$ .

While multiplying 2.5 and 1.25, you will first multiply 25 and 125. For placing the decimal in the product obtained, you will count  $1 + 2 = 3$  (Why?) digits starting from the rightmost digit. Thus,  $2.5 \times 1.25 = 3.225$

Find  $2.7 \times 1.35$ .

### TRY THESE



- Find: (i)  $2.7 \times 4$  (ii)  $1.8 \times 1.2$  (iii)  $2.3 \times 4.35$
- Arrange the products obtained in (1) in descending order.

**EXAMPLE 7** The side of an equilateral triangle is 3.5 cm. Find its perimeter.

**SOLUTION** All the sides of an equilateral triangle are equal.

So, length of each side = 3.5 cm

Thus, perimeter =  $3 \times 3.5$  cm = 10.5 cm

**EXAMPLE 8** The length of a rectangle is 7.1 cm and its breadth is 2.5 cm. What is the area of the rectangle?

**SOLUTION** Length of the rectangle = 7.1 cm

Breadth of the rectangle = 2.5 cm

Therefore, area of the rectangle =  $7.1 \times 2.5$  cm<sup>2</sup> = 17.75 cm<sup>2</sup>

### 2.6.1 Multiplication of Decimal Numbers by 10, 100 and 1000

Reshma observed that  $2.3 = \frac{23}{10}$  whereas  $2.35 = \frac{235}{100}$ . Thus, she found that depending on the position of the decimal point the decimal number can be converted to a fraction with denominator 10 or 100. She wondered what would happen if a decimal number is multiplied by 10 or 100 or 1000.

Let us see if we can find a pattern of multiplying numbers by 10 or 100 or 1000.

Have a look at the table given below and fill in the blanks:

$1.76 \times 10 = \frac{176}{100} \times 10 = 17.6$	$2.35 \times 10 = \underline{\hspace{2cm}}$	$12.356 \times 10 = \underline{\hspace{2cm}}$
$1.76 \times 100 = \frac{176}{100} \times 100 = 176 \text{ or } 176.0$	$2.35 \times 100 = \underline{\hspace{2cm}}$	$12.356 \times 100 = \underline{\hspace{2cm}}$
$1.76 \times 1000 = \frac{176}{100} \times 1000 = 1760 \text{ or } 1760.0$	$2.35 \times 1000 = \underline{\hspace{2cm}}$	$12.356 \times 1000 = \underline{\hspace{2cm}}$
$0.5 \times 10 = \frac{5}{10} \times 10 = 5 \quad ; \quad 0.5 \times 100 = \underline{\hspace{2cm}} \quad ; \quad 0.5 \times 1000 = \underline{\hspace{2cm}}$		

Observe the shift of the decimal point of the products in the table. Here the numbers are multiplied by 10, 100 and 1000. In  $1.76 \times 10 = 17.6$ , the digits are same i.e., 1, 7 and 6. Do you observe this in other products also? Observe 1.76 and 17.6. To which side has the decimal point shifted, right or left? The decimal point has shifted to the right by one place. Note that 10 has one zero over 1.

In  $1.76 \times 100 = 176.0$ , observe 1.76 and 176.0. To which side and by how many digits has the decimal point shifted? The decimal point has shifted to the right by two places.

Note that 100 has two zeros over one.

Do you observe similar shifting of decimal point in other products also?

So we say, *when a decimal number is multiplied by 10, 100 or 1000, the digits in the product are same as in the decimal number but the decimal point in the product is shifted to the right by as many places as there are zeros over one.*

Based on these observations we can now say

$$0.07 \times 10 = 0.7, 0.07 \times 100 = 7 \text{ and } 0.07 \times 1000 = 70.$$

Can you now tell  $2.97 \times 10 = ?$   $2.97 \times 100 = ?$   $2.97 \times 1000 = ?$

Can you now help Reshma to find the total amount i.e., ₹  $8.50 \times 150$ , that she has to pay?

#### TRY THESE

- Find: (i)  $0.3 \times 10$   
 (ii)  $1.2 \times 100$   
 (iii)  $56.3 \times 1000$

## EXERCISE 2.6



1. Find:

- (i)  $0.2 \times 6$       (ii)  $8 \times 4.6$       (iii)  $2.71 \times 5$       (iv)  $20.1 \times 4$   
 (v)  $0.05 \times 7$       (vi)  $211.02 \times 4$       (vii)  $2 \times 0.86$

2. Find the area of rectangle whose length is 5.7cm and breadth is 3 cm.

3. Find:

- (i)  $1.3 \times 10$       (ii)  $36.8 \times 10$       (iii)  $153.7 \times 10$       (iv)  $168.07 \times 10$   
 (v)  $31.1 \times 100$       (vi)  $156.1 \times 100$       (vii)  $3.62 \times 100$       (viii)  $43.07 \times 100$   
 (ix)  $0.5 \times 10$       (x)  $0.08 \times 10$       (xi)  $0.9 \times 100$       (xii)  $0.03 \times 1000$

4. A two-wheeler covers a distance of 55.3 km in one litre of petrol. How much distance will it cover in 10 litres of petrol?

5. Find:

- (i)  $2.5 \times 0.3$       (ii)  $0.1 \times 51.7$       (iii)  $0.2 \times 316.8$       (iv)  $1.3 \times 3.1$   
 (v)  $0.5 \times 0.05$       (vi)  $11.2 \times 0.15$       (vii)  $1.07 \times 0.02$   
 (viii)  $10.05 \times 1.05$       (ix)  $101.01 \times 0.01$       (x)  $100.01 \times 1.1$

## 2.7 DIVISION OF DECIMAL NUMBERS

Savita was preparing a design to decorate her classroom. She needed a few coloured strips of paper of length 1.9 cm each. She had a strip of coloured paper of length 9.5 cm. How many pieces of the required length will she get out of this strip? She thought it would

be  $\frac{9.5}{1.9}$  cm. Is she correct?

Both 9.5 and 1.9 are decimal numbers. So we need to know the division of decimal numbers too!



### 2.7.1 Division by 10, 100 and 1000

Let us find the division of a decimal number by 10, 100 and 1000.

Consider  $31.5 \div 10$ .

$$31.5 \div 10 = \frac{315}{10} \times \frac{1}{10} = \frac{315}{100} = 3.15$$

$$\text{Similarly, } 31.5 \div 100 = \frac{315}{10} \times \frac{1}{100} = \frac{315}{1000} = 0.315$$

Let us see if we can find a pattern for dividing numbers by 10, 100 or 1000. This may help us in dividing numbers by 10, 100 or 1000 in a shorter way.

$31.5 \div 10 = 3.15$	$231.5 \div 10 = \underline{\hspace{1cm}}$	$1.5 \div 10 = \underline{\hspace{1cm}}$	$29.36 \div 10 = \underline{\hspace{1cm}}$
$31.5 \div 100 = 0.315$	$231.5 \div 100 = \underline{\hspace{1cm}}$	$1.5 \div 100 = \underline{\hspace{1cm}}$	$29.36 \div 100 = \underline{\hspace{1cm}}$
$31.5 \div 1000 = 0.0315$	$231.5 \div 1000 = \underline{\hspace{1cm}}$	$1.5 \div 1000 = \underline{\hspace{1cm}}$	$29.36 \div 1000 = \underline{\hspace{1cm}}$



Take  $31.5 \div 10 = 3.15$ . In 31.5 and 3.15, the digits are same i.e., 3, 1, and 5 but the decimal point has shifted in the quotient. To which side and by how many digits? The decimal point has shifted to the left by one place. Note that 10 has one zero over 1.

Consider now  $31.5 \div 100 = 0.315$ . In 31.5 and 0.315 the digits are same, but what about the decimal point in the quotient? It has shifted to the left by two places. Note that 100 has two zeros over 1.

So we can say that, *while dividing a number by 10, 100 or 1000, the digits of the number and the quotient are same but the decimal point in the quotient shifts to the left by as many places as there are zeros over 1.* Using this observation let us now quickly find:  $2.38 \div 10 = 0.238$ ,  $2.38 \div 100 = 0.0238$ ,  $2.38 \div 1000 = 0.00238$

### 2.7.2 Division of a Decimal Number by a Whole Number

Let us find  $\frac{6.4}{2}$ . Remember we also write it as  $6.4 \div 2$ .

So,  $6.4 \div 2 = \frac{64}{10} \div 2 = \frac{64}{10} \times \frac{1}{2}$  as learnt in fractions.

$$= \frac{64 \times 1}{10 \times 2} = \frac{1 \times 64}{10 \times 2} = \frac{1}{10} \times \frac{64}{2} = \frac{1}{10} \times 32 = \frac{32}{10} = 3.2$$

Or, let us first divide 64 by 2. We get 32. There is one digit to the right of the decimal point in 6.4. Place the decimal in 32 such that there would be one digit to its right. We get 3.2 again.

To find  $19.5 \div 5$ , first find  $195 \div 5$ . We get 39. There is one digit to the right of the decimal point in 19.5. Place the decimal point in 39 such that there would be one digit to its right. You will get 3.9.

Now,  $12.96 \div 4 = \frac{1296}{100} \div 4 = \frac{1296}{100} \times \frac{1}{4} = \frac{1}{100} \times \frac{1296}{4} = \frac{1}{100} \times 324 = 3.24$

Or, divide 1296 by 4. You get 324. There are two digits to the right of the decimal in 12.96. Making similar placement of the decimal in 324, you will get 3.24.

Note that here and in the next section, we have considered only those divisions in which, ignoring the decimal, the number would be completely divisible by another number to give remainder zero. Like, in  $19.5 \div 5$ , the number 195 when divided by 5, leaves remainder zero.

However, there are situations in which the number may not be completely divisible by another number, i.e., we may not get remainder zero. For example,  $195 \div 7$ . We deal with such situations in later classes.

Thus,  $40.86 \div 6 = 6.81$

#### TRY THESE



- Find: (i)  $235.4 \div 10$   
 (ii)  $235.4 \div 100$   
 (iii)  $235.4 \div 1000$

#### TRY THESE

- (i)  $35.7 \div 3 = ?$ ;  
 (ii)  $25.5 \div 3 = ?$



#### TRY THESE

- (i)  $43.15 \div 5 = ?$ ;  
 (ii)  $82.44 \div 6 = ?$

#### TRY THESE

- Find: (i)  $15.5 \div 5$   
 (ii)  $126.35 \div 7$

**EXAMPLE 9** Find the average of 4.2, 3.8 and 7.6.

**SOLUTION** The average of 4.2, 3.8 and 7.6 is  $\frac{4.2+3.8+7.6}{3} = 5.2$ .

### 2.7.3 Division of a Decimal Number by another Decimal Number

Let us find  $\frac{25.5}{0.5}$  i.e.,  $25.5 \div 0.5$ .

We have  $25.5 \div 0.5 = \frac{255}{10} \div \frac{5}{10} = \frac{255}{10} \times \frac{10}{5} = 51$ . Thus,  $25.5 \div 0.5 = 51$

What do you observe? For  $\frac{25.5}{0.5}$ , we find that there is one digit to the right of the decimal in 0.5. This could be converted to whole number by dividing by 10. Accordingly 25.5 was also converted to a fraction by dividing by 10.

Or, we say the decimal point was shifted by one place to the right in 0.5 to make it 5. So, there was a shift of one decimal point to the right in 25.5 also to make it 255.

Thus,  $22.5 \div 1.5 = \frac{225}{15} = 15$

Find  $\frac{20.3}{0.7}$  and  $\frac{15.2}{0.8}$  in a similar way.

Let us now find  $20.55 \div 1.5$ .

We can write it as  $205.5 \div 15$ , as discussed above. We get 13.7. Find  $\frac{3.96}{0.4}$ ,  $\frac{2.31}{0.3}$ .

Consider now,  $\frac{33.725}{0.25}$ . We can write it as  $\frac{3372.5}{25}$  (How?) and we get the quotient as 134.9. How will you find  $\frac{27}{0.03}$ ? We know that 27 can be written as 27.0.

So,  $\frac{27}{0.03} = \frac{27.00}{0.03} = \frac{2700}{3} = ?$

**EXAMPLE 10** Each side of a regular polygon is 2.5 cm in length. The perimeter of the polygon is 12.5 cm. How many sides does the polygon have?

**SOLUTION** The perimeter of a regular polygon is the sum of the lengths of all its equal sides = 12.5 cm.

Length of each side = 2.5 cm. Thus, the number of sides =  $\frac{12.5}{2.5} = \frac{125}{25} = 5$

The polygon has 5 sides.

#### TRY THESE

Find: (i)  $\frac{7.75}{0.25}$  (ii)  $\frac{42.8}{0.02}$  (iii)  $\frac{5.6}{1.4}$

**EXAMPLE 11** A car covers a distance of 89.1 km in 2.2 hours. What is the average distance covered by it in 1 hour?

**SOLUTION** Distance covered by the car = 89.1 km.

Time required to cover this distance = 2.2 hours.

So distance covered by it in 1 hour =  $\frac{89.1}{2.2} = \frac{891}{22} = 40.5$  km.

## EXERCISE 2.7

1. Find:

(i)  $0.4 \div 2$

(ii)  $0.35 \div 5$

(iii)  $2.48 \div 4$

(iv)  $65.4 \div 6$

(v)  $651.2 \div 4$

(vi)  $14.49 \div 7$

(vii)  $3.96 \div 4$

(viii)  $0.80 \div 5$

2. Find:

(i)  $4.8 \div 10$

(ii)  $52.5 \div 10$

(iii)  $0.7 \div 10$

(iv)  $33.1 \div 10$

(v)  $272.23 \div 10$

(vi)  $0.56 \div 10$

(vii)  $3.97 \div 10$

3. Find:

(i)  $2.7 \div 100$

(ii)  $0.3 \div 100$

(iii)  $0.78 \div 100$

(iv)  $432.6 \div 100$

(v)  $23.6 \div 100$

(vi)  $98.53 \div 100$

4. Find:

(i)  $7.9 \div 1000$

(ii)  $26.3 \div 1000$

(iii)  $38.53 \div 1000$

(iv)  $128.9 \div 1000$

(v)  $0.5 \div 1000$

5. Find:

(i)  $7 \div 3.5$

(ii)  $36 \div 0.2$

(iii)  $3.25 \div 0.5$

(iv)  $30.94 \div 0.7$

(v)  $0.5 \div 0.25$

(vi)  $7.75 \div 0.25$

(vii)  $76.5 \div 0.15$

(viii)  $37.8 \div 1.4$

(ix)  $2.73 \div 1.3$

6. A vehicle covers a distance of 43.2 km in 2.4 litres of petrol. How much distance will it cover in one litre of petrol?



## WHAT HAVE WE DISCUSSED?

- We have learnt about fractions and decimals alongwith the operations of addition and subtraction on them, in the earlier class.
- We now study the operations of multiplication and division on fractions as well as on decimals.
- We have learnt how to multiply fractions. Two fractions are multiplied by multiplying their numerators and denominators separately and writing the product as

$$\frac{\text{product of numerators}}{\text{product of denominators}}. \text{ For example, } \frac{2}{3} \times \frac{5}{7} = \frac{2 \times 5}{3 \times 7} = \frac{10}{21}.$$

- A fraction acts as an operator 'of'. For example,  $\frac{1}{2}$  of 2 is  $\frac{1}{2} \times 2 = 1$ .

5. (a) The product of two proper fractions is less than each of the fractions that are multiplied.  
 (b) The product of a proper and an improper fraction is less than the improper fraction and greater than the proper fraction.  
 (c) The product of two improper fractions is greater than the two fractions.
6. A reciprocal of a fraction is obtained by inverting it upside down.
7. We have seen how to divide two fractions.

- (a) While dividing a whole number by a fraction, we multiply the whole number with the reciprocal of that fraction.

$$\text{For example, } 2 \div \frac{3}{5} = 2 \times \frac{5}{3} = \frac{10}{3}$$

- (b) While dividing a fraction by a whole number we multiply the fraction by the reciprocal of the whole number.

$$\text{For example, } \frac{2}{3} \div 7 = \frac{2}{3} \times \frac{1}{7} = \frac{2}{21}$$

- (c) While dividing one fraction by another fraction, we multiply the first fraction by

$$\text{the reciprocal of the other. So, } \frac{2}{3} \div \frac{5}{7} = \frac{2}{3} \times \frac{7}{5} = \frac{14}{15}.$$

8. We also learnt how to multiply two decimal numbers. While multiplying two decimal numbers, first multiply them as whole numbers. Count the number of digits to the right of the decimal point in both the decimal numbers. Add the number of digits counted. Put the decimal point in the product by counting the digits from its rightmost place. The count should be the sum obtained earlier.

$$\text{For example, } 0.5 \times 0.7 = 0.35$$

9. To multiply a decimal number by 10, 100 or 1000, we move the decimal point in the number to the right by as many places as there are zeros over 1.

$$\text{Thus } 0.53 \times 10 = 5.3, \quad 0.53 \times 100 = 53, \quad 0.53 \times 1000 = 530$$

10. We have seen how to divide decimal numbers.

- (a) To divide a decimal number by a whole number, we first divide them as whole numbers. Then place the decimal point in the quotient as in the decimal number.

$$\text{For example, } 8.4 \div 4 = 2.1$$

Note that here we consider only those divisions in which the remainder is zero.

- (b) To divide a decimal number by 10, 100 or 1000, shift the digits in the decimal number to the left by as many places as there are zeros over 1, to get the quotient.

$$\text{So, } 23.9 \div 10 = 2.39, 23.9 \div 100 = 0.239, \quad 23.9 \div 1000 = 0.0239$$

- (c) While dividing two decimal numbers, first shift the decimal point to the right by equal number of places in both, to convert the divisor to a whole number. Then divide. Thus,  $2.4 \div 0.2 = 24 \div 2 = 12$ .

